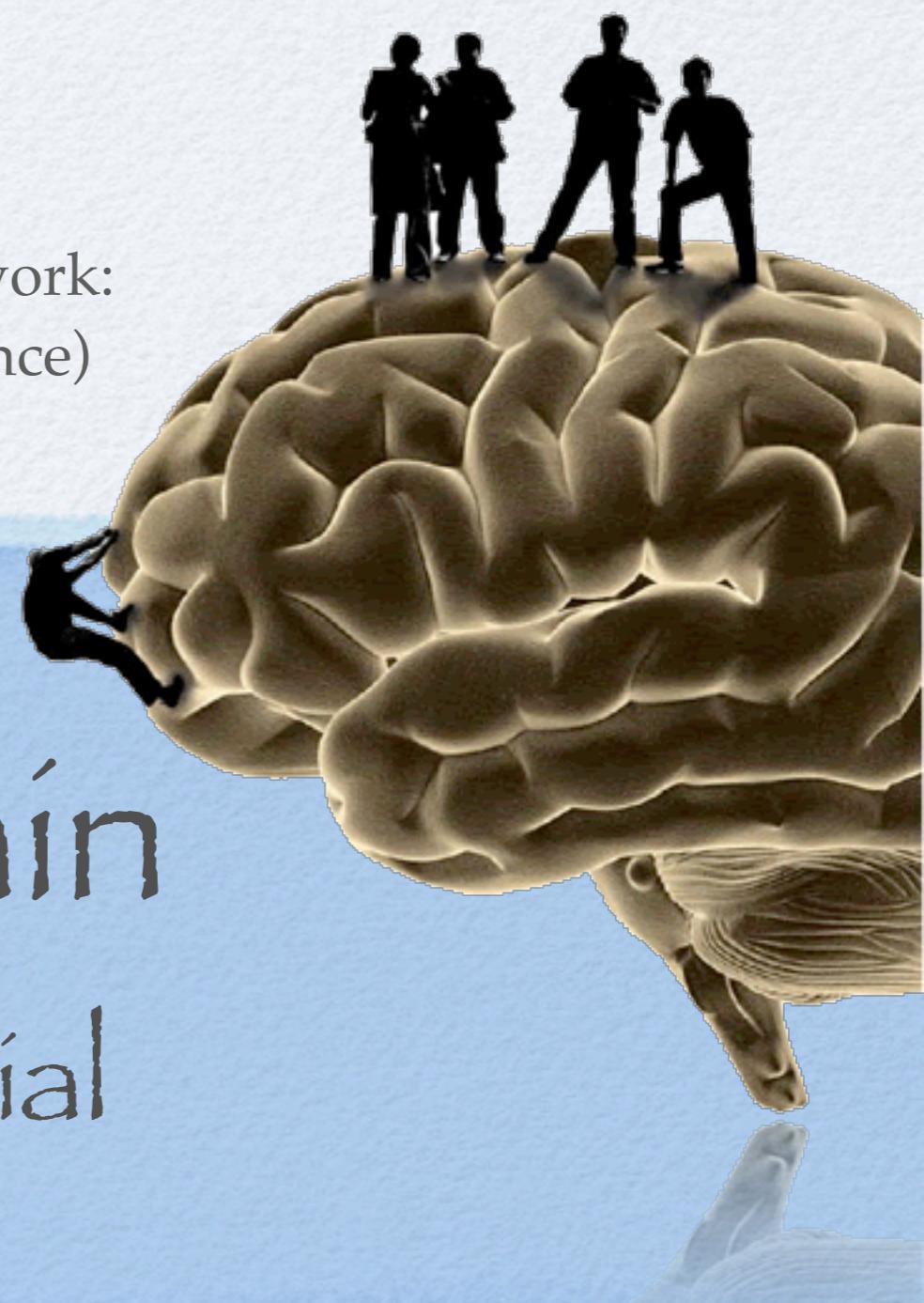


(Nengo and the Neural Engineering Framework:  
Connecting Cognitive Theory to Neuroscience)

# How to build a brain

## Cogsci 2010 Tutorial



Terry Stewart & Chris Eliasmith

Centre for Theoretical Neuroscience

University of Waterloo

# There are animals



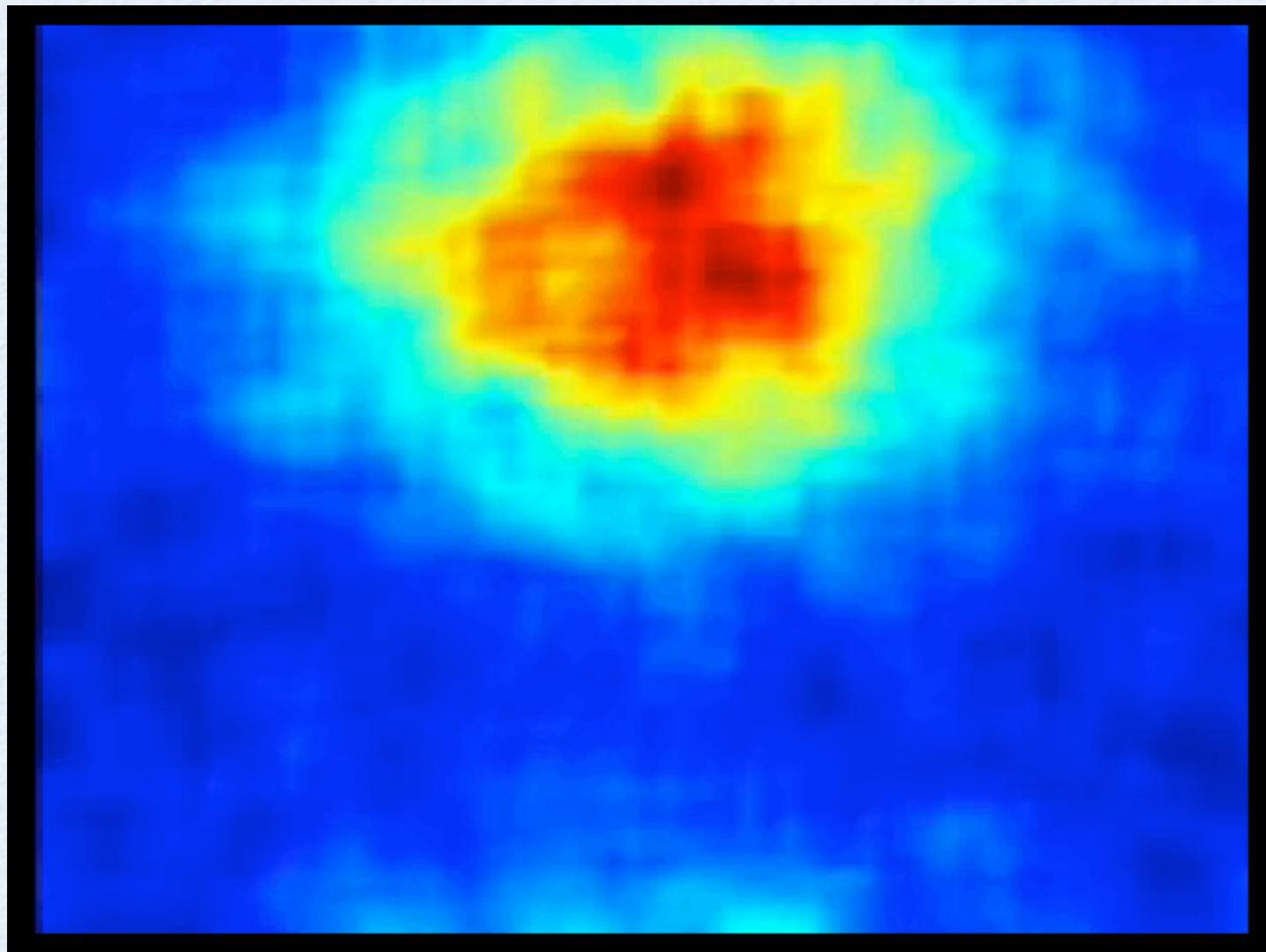
# who behave



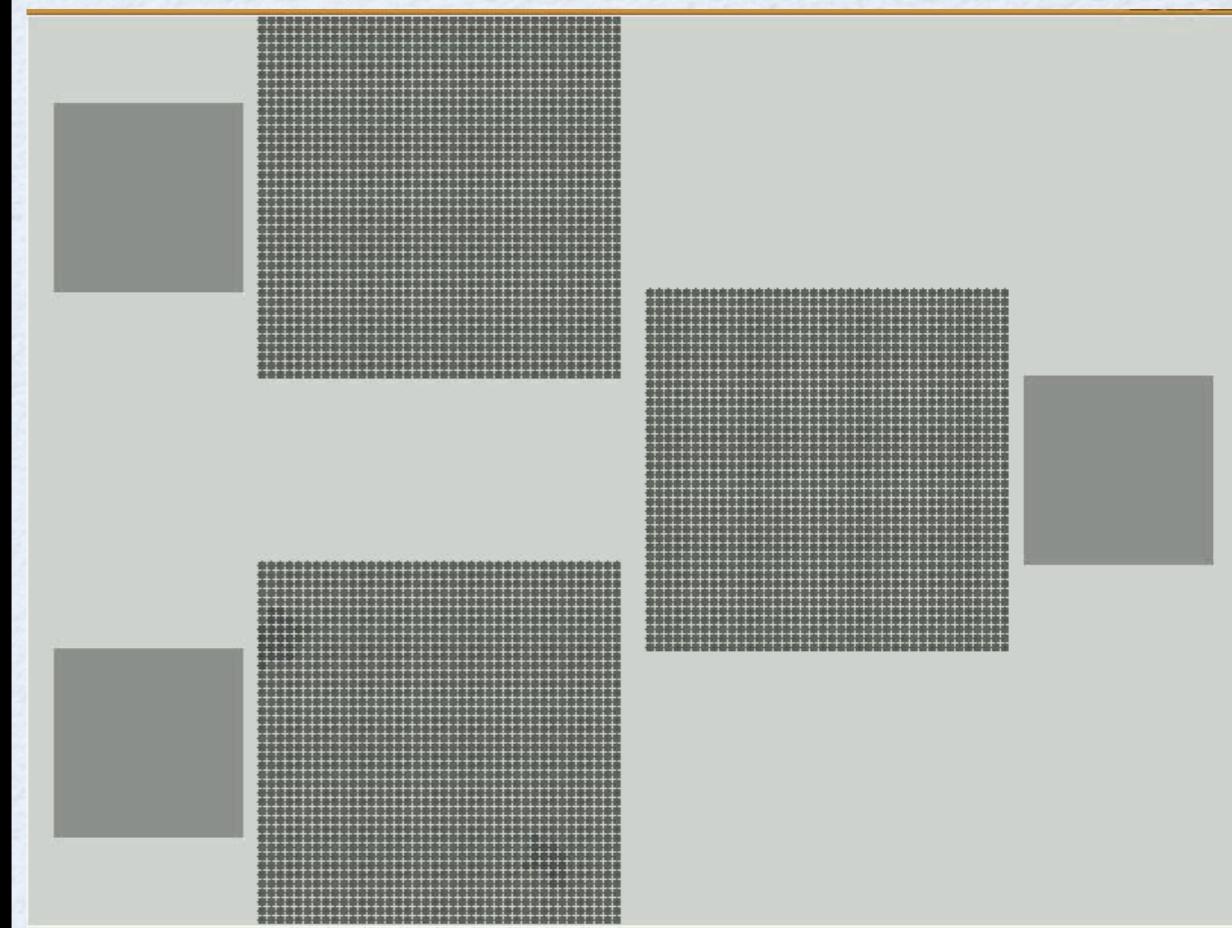
brains  
think?



# which we want to model



Path integration



Neural binding

# Compelling reasons for neurons

- Better contact with more data (single, multi-electrode, LFP, fMRI, ERP, behavioural, etc.)
- Explanations for previous assumptions (e.g. Why a 50ms time step? Why limited productivity? etc.)
- Wider range of manipulations (e.g., brain damage, genetic alteration, degeneration, stimulation, etc.)
- **Others?** (Neurons limit computational alternatives, neurons impose dynamic constraints, anatomy imposes topological constraints, etc.)

# Today

- Introduction
  - Who we are
  - Who you are, why you're here
- Six topics (theory followed by hands-on simulation)
  1. 1D representation
  2. linear transformation
  3. nonlinear transformation
  4. dynamics
  5. symbol manipulation
  6. applications (time permitting)

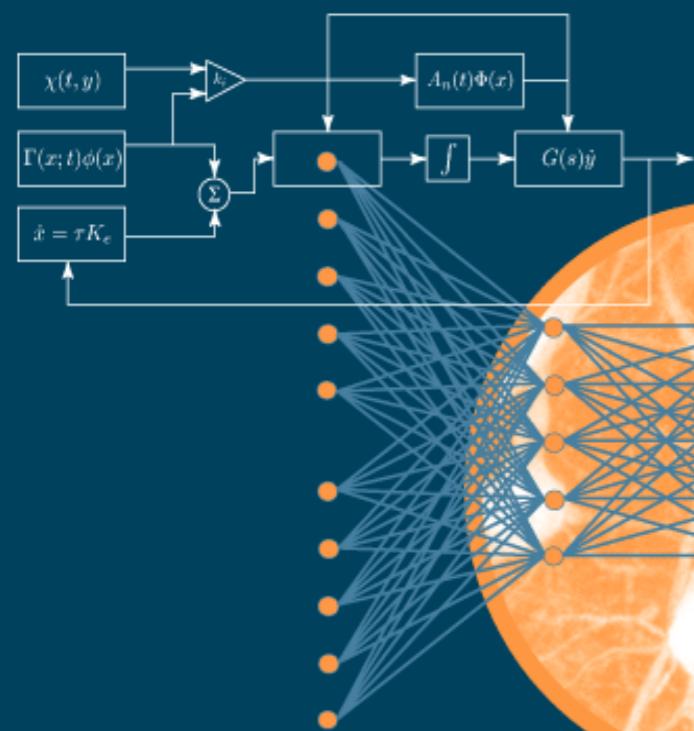
Please Interrupt!

# Theory

## Neural Engineering

COMPUTATION, REPRESENTATION, AND DYNAMICS  
IN NEUROBIOLOGICAL SYSTEMS

Chris Eliasmith and Charles H. Anderson



## Neural Engineering Framework (NEF)

Given:

- Information processing task
- Hardware description

Produce:

- Neural mechanism

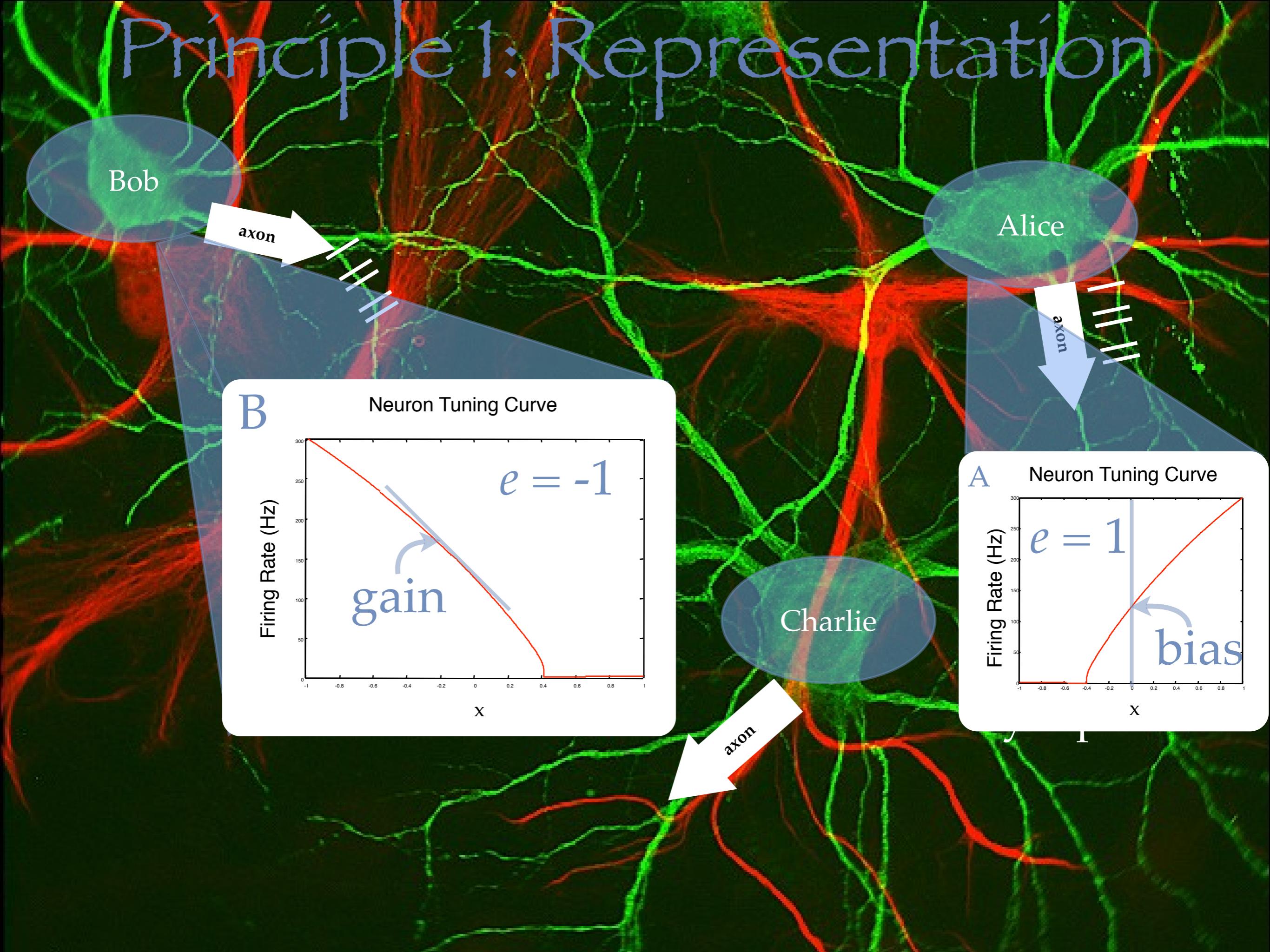
# The NEF

- A theory, like Newton's theory of motion:
  - Three basic principles
    - Representation, Transformation, Dynamics
    - General, unified approach
    - Quantitative
    - Wrong!

# Representation

- Lossless code (e.g. Morse code):
  - Encoding:  $a = f(x)$
  - Decoding:  $x = f^{-1}(a)$
- Otherwise (e.g. A/D conversion):
  - Decoding:  $\hat{x} = g(a) \approx f^{-1}(a)$

# Principle 1: Representation



# Nonlinear encoding

- More specifically, we know:

$$J(x) = \alpha x + J^{bias}$$

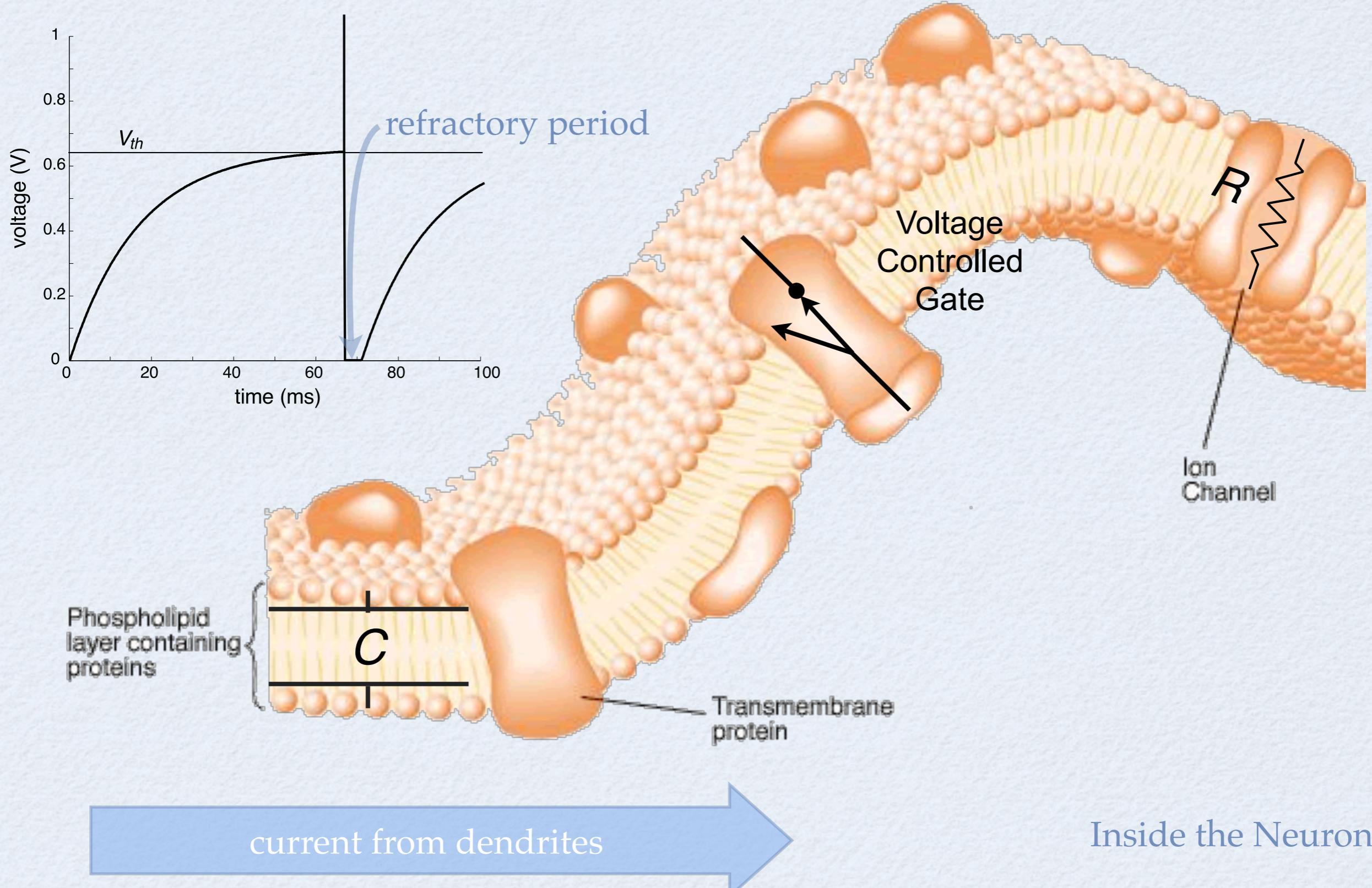
- So

$$a_i(x) = G_i [\alpha x + J^{bias}]$$

- $G_i$  can be any neural model
  - conductance; rate; leaky integrate-and-fire (LIF)

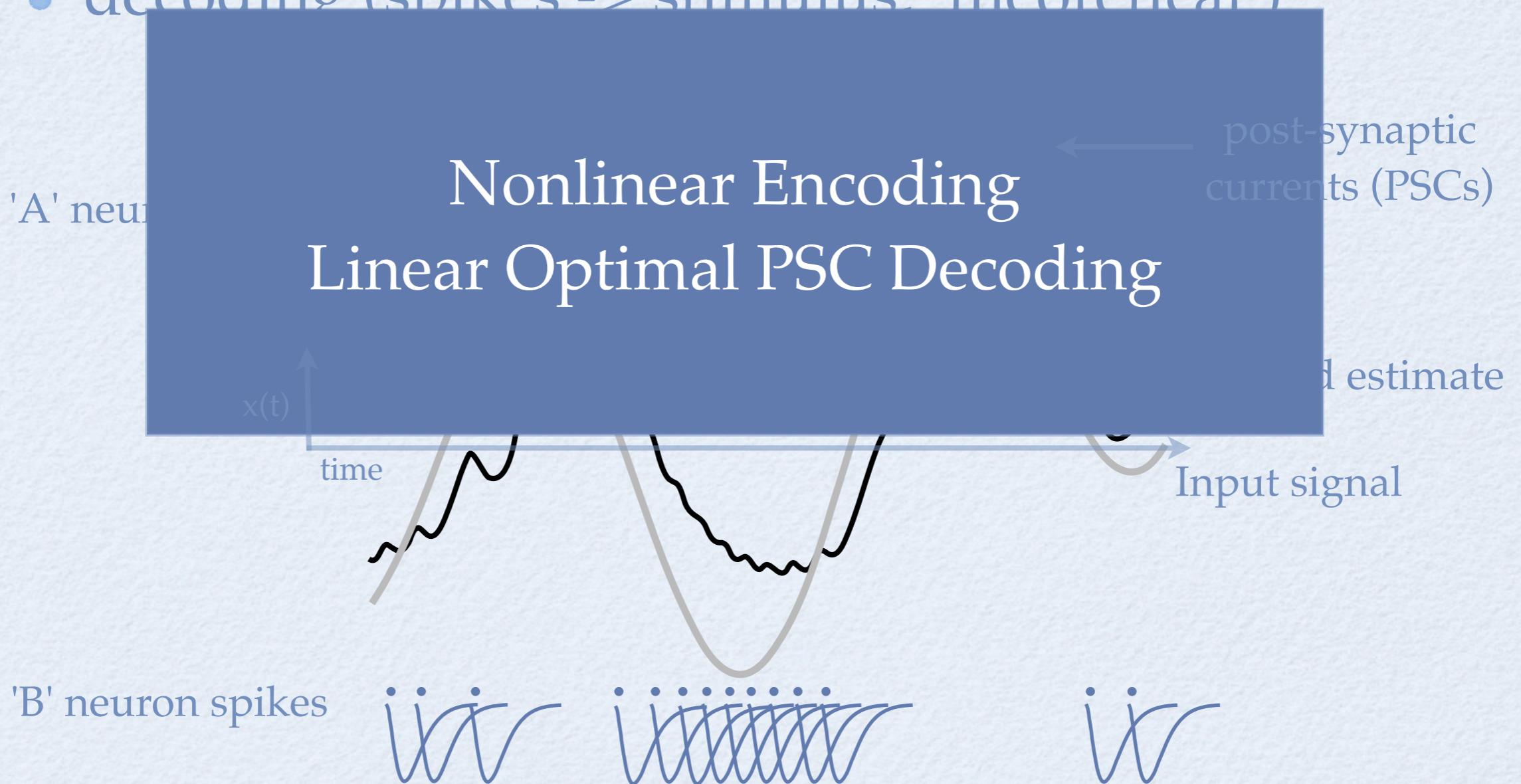
# Leaky integrate-and-fire (LIF) model

Outside the Neuron

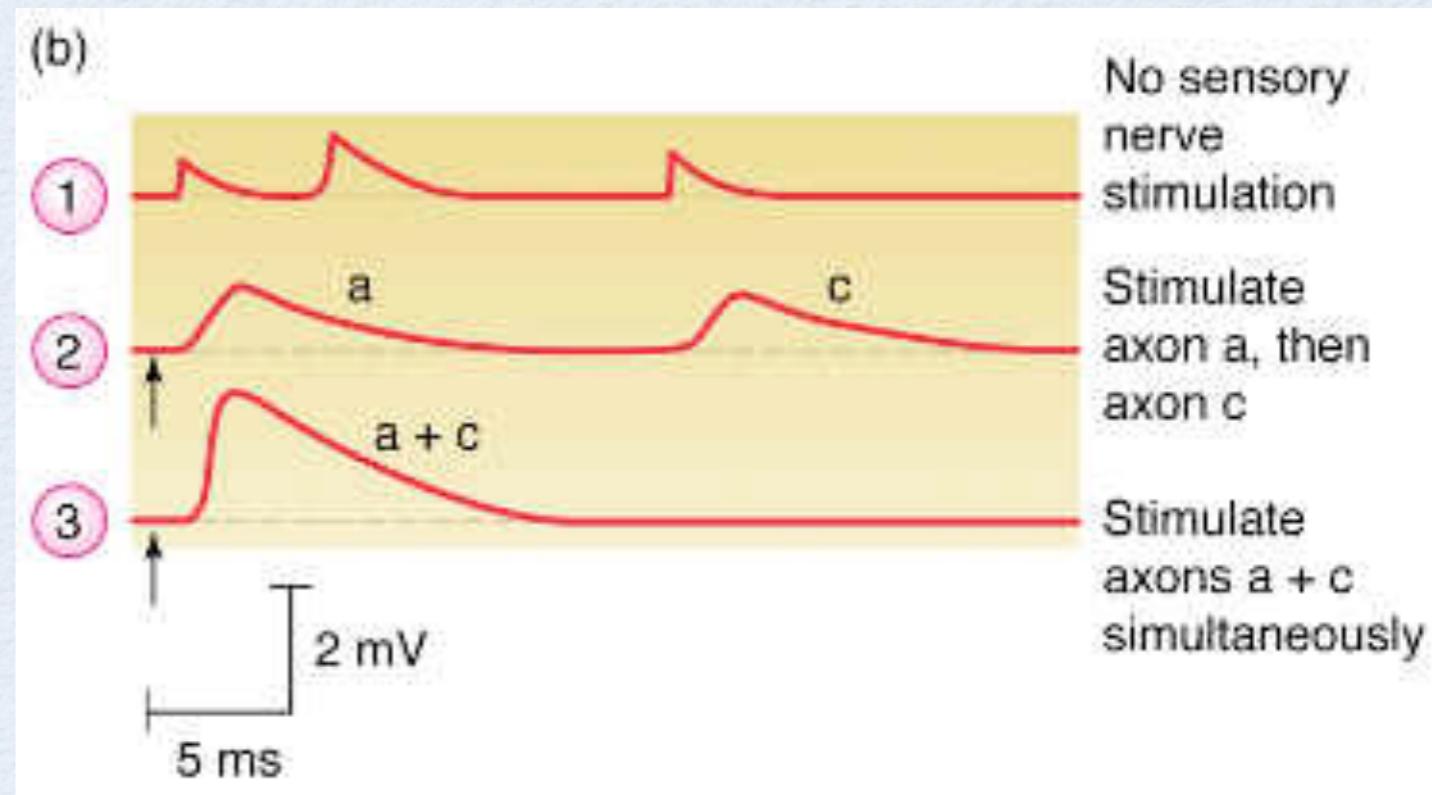
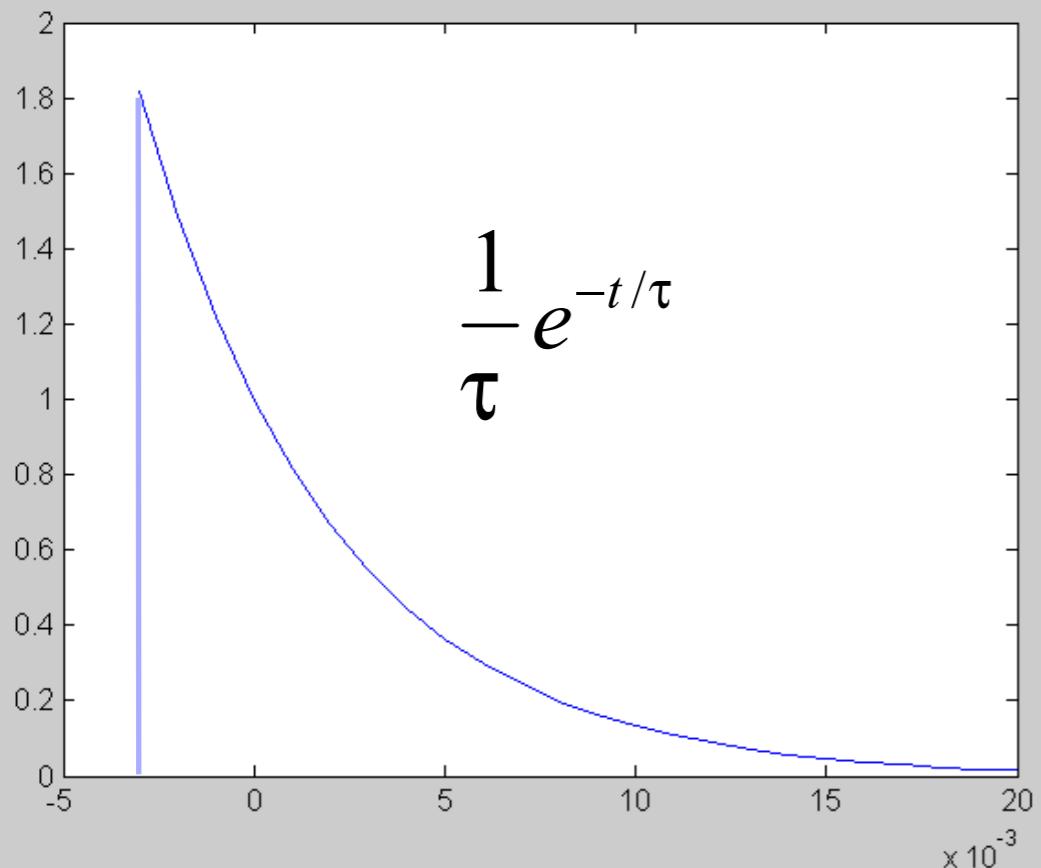


# Principle 1: Representation

- Need two procedures to define representation
  - encoding (stimulus -> spikes)
  - decoding (spikes -> stimulus: ‘theoretical’)



# Typical PSCs



From: <http://www.zoo.utoronto.ca/berry/zoo252/19/lect9.htm>

# Optimal linear decoding

- Linear:

$$\hat{x} = \sum_i a_i(x) \phi_i$$

- Note: Must know tuning curves,  $a_i$
- Q: How to find decoders?
- A: Minimize  $\langle (x - \hat{x})^2 \rangle_x$

# Sources of Noise

- Axonal jitter
- Neurotransmitter vesicle release failures
- Different amount of transmitter in each vesicle
- Thermal noise (minor)
- Ion channel noise (the number of channels open or closed fluctuates)
- Network effects
- See also <http://diwww.epfl.ch/~gerstner/SPNM/node33.html>

# Noise

- So, we must consider the decoding under noise:

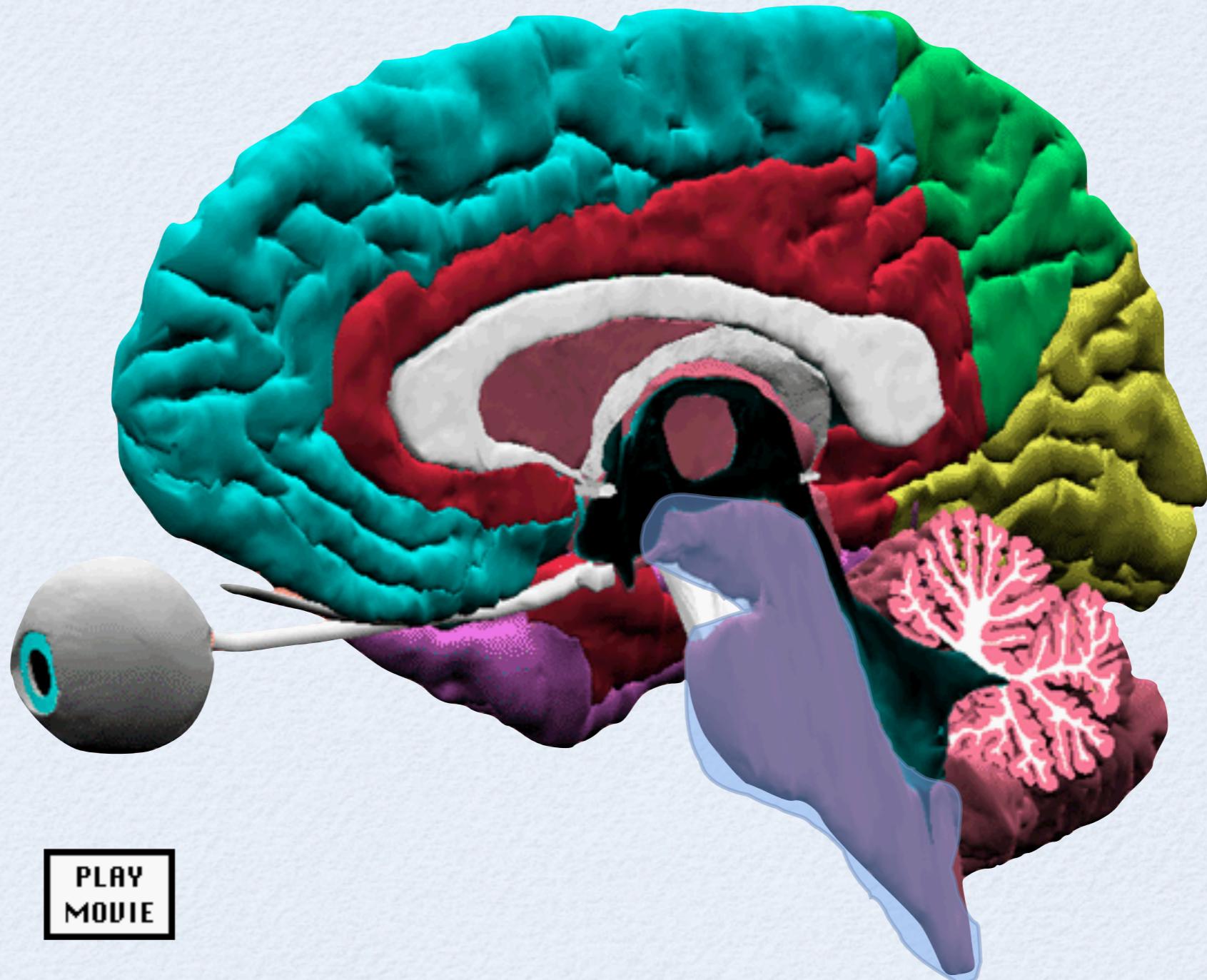
$$\hat{x} = \sum_{i=1}^N (a_i(x) + \eta_i) \phi_i$$

- Hence, minimize

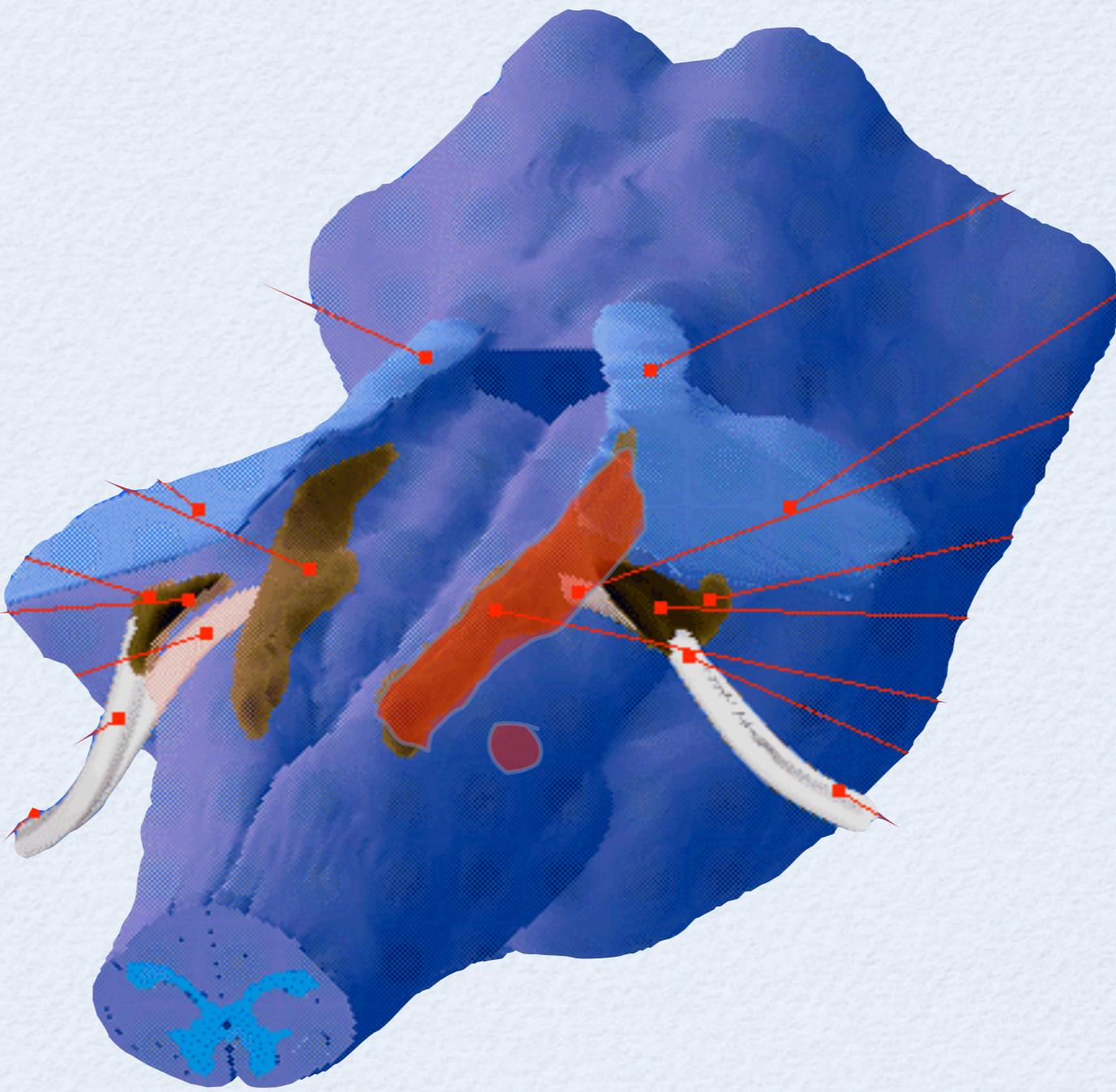
$$\langle (x - \hat{x})^2 \rangle_{x, \eta_i}$$

# Brain stem

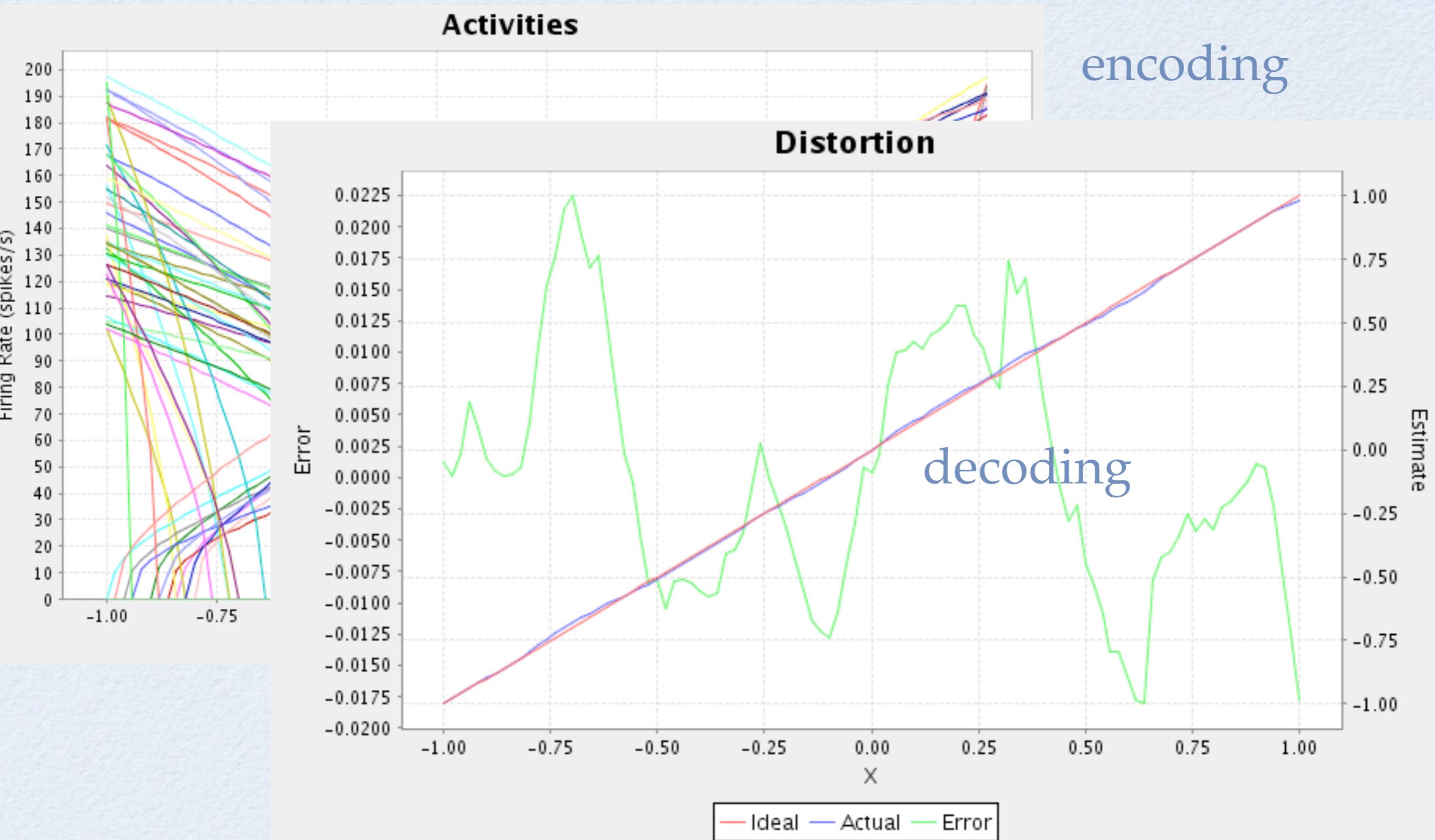
- The neural integrator represents eye position



# NPH and Vestibular nuclei



# Population tuning



# Error with/without noise\*

